

Exercise 6.1 (Revised) - Chapter 6 - Triangles - Ncert Solutions class 10 - Maths

Updated On 11-02-2025 By Lithanya

Chapter 6 Triangles NCERT Solutions Class 10 Maths: Simplify Concepts & Ace Exams

Ex 6.1 Question 1.

Fill in the blanks using the correct word given in brackets:

- (i) All circles are _____. (congruent, similar)
- (ii) All squares are _____. (similar, congruent)
- (iii) All _____ triangles are similar. (isosceles, equilateral)
- (iv) Two polygons of the same number of sides are similar, if (a) their corresponding angles are _____ and (b) their corresponding sides are _____. (equal, proportional)

Answer.

- (i) similar
- (ii) similar
- (iii) equilateral
- (iv) equal, proportional

Ex 6.1 Question 2.

Give two different examples of pair of:

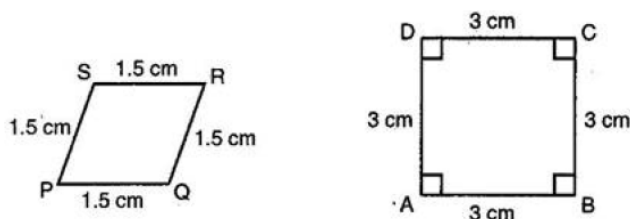
- (i) similar figures
- (ii) non-similar figures

Answer.

- (i) Two different examples of a pair of similar figures are:
 - (a) Any two rectangles
 - (b) Any two squares
- (ii) Two different examples of a pair of non-similar figures are:
 - (a) A scalene and an equilateral triangle
 - (b) An equilateral triangle and a right angled triangle

Ex 6.1 Question 3.

State whether the following quadrilaterals are similar or not:



Answer.

On looking at the given figures of the quadrilaterals, we can say that they are not similar because their angles are not equal.



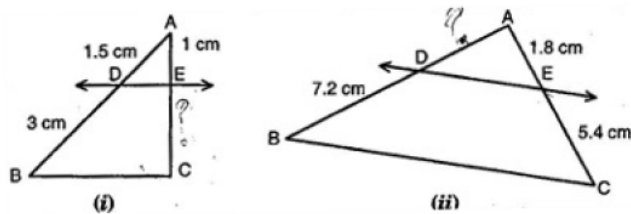
Exercise 6.2 (Revised) - Chapter 6 - Triangles - Ncert Solutions class 10 - Maths

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Chapter 6 Triangles NCERT Solutions Class 10 Maths: Simplify Concepts & Ace Exams

Ex 6.2 Question 1.

In figure (i) and (ii), $DE \parallel BC$. Find EC in (i) and AD in (ii).



Answer.

(i) Since $DE \parallel BC$,

$$\therefore \frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{1.5}{3} = \frac{1}{EC}$$

$$\Rightarrow EC = \frac{3}{1.5}$$

$$\Rightarrow EC = 2 \text{ cm}$$

(ii) Since $DE \parallel BC$,

$$\therefore \frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{AD}{7.2} = \frac{1.8}{5.4}$$

$$\Rightarrow AD = \frac{1.8 \times 7.2}{5.4}$$

$$\Rightarrow EC = 2.4 \text{ cm}$$

Ex 6.2 Question 2.

E and F are points on the sides PQ and PR respectively of a $\triangle PQR$. For each of the following cases, state whether $EF \parallel QR$:

(i) $PE = 3.9 \text{ cm}$, $EQ = 4 \text{ cm}$, $PF = 3.6 \text{ cm}$ and $FR = 2.4 \text{ cm}$

(ii) $PE = 4 \text{ cm}$, $QE = 4.5 \text{ cm}$, $PF = 8 \text{ cm}$ and $RF = 9 \text{ cm}$

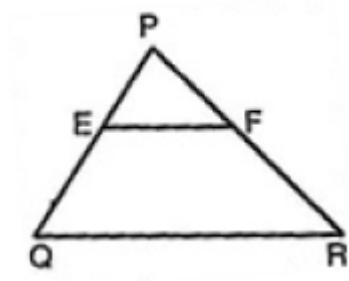
(iii) $PQ = 1.28 \text{ cm}$, $PR = 2.56 \text{ cm}$, $PE = 0.18 \text{ cm}$ and $PF = 0.36 \text{ cm}$

Answer.

(i) Given: $PE = 3.9 \text{ cm}$, $EQ = 4 \text{ cm}$, $PF = 3.6 \text{ cm}$ and $FR = 2.4 \text{ cm}$

$$\text{Now, } \frac{PE}{EQ} = \frac{3.9}{4} = 0.975$$





$$\text{And } \frac{PF}{FR} = \frac{3.6}{2.4} = 1.2 \text{ cm}$$

$$\therefore \frac{PE}{EQ} \neq \frac{PF}{FR}$$

Therefore, EF does not divide the sides PQ and PR of $\triangle PQR$ in the same ratio.

\therefore EF is not parallel to QR.

(ii) Given: PE = 4 cm, QE = 4.5 cm, PF = 8 cm and RF = 9 cm

$$\text{Now, } \frac{PE}{EQ} = \frac{4}{4.5} = \frac{8}{9} \text{ cm}$$

$$\text{And } \frac{PF}{FR} = \frac{8}{9} \text{ cm}$$

$$\therefore \frac{PE}{EQ} = \frac{PF}{FR}$$

Therefore, EF divides the sides PQ and PR of $\triangle PQR$ in the same ratio.

\therefore EF is parallel to QR.

(iii) Given: PQ = 1.28 cm, PR = 2.56 cm, PE = 0.18 cm and PF = 0.36 cm

$$\Rightarrow EQ = PQ - PE = 1.28 - 0.18 = 1.10 \text{ cm}$$

$$\text{And } ER = PR - PF = 2.56 - 0.36 = 2.20 \text{ cm}$$

$$\text{Now, } \frac{PE}{EQ} = \frac{0.18}{1.10} = \frac{18}{110} = \frac{9}{55} \text{ cm}$$

$$\text{And } \frac{PF}{FR} = \frac{0.36}{2.20} = \frac{36}{220} = \frac{9}{55} \text{ cm}$$

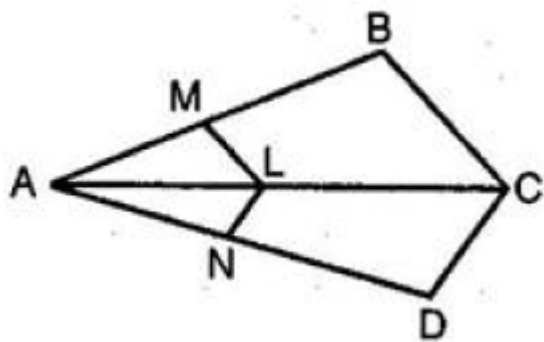
$$\therefore \frac{PE}{EQ} = \frac{PF}{FR}$$

Therefore, EF divides the sides PQ and PR of $\triangle PQR$ in the same ratio.

\therefore EF is parallel to QR.

Ex 6.2 Question 3.

In figure, if $LM \parallel CB$ and $LN \parallel CD$, prove that $\frac{AM}{AB} = \frac{AN}{AD}$.



Answer.

In $\triangle ABC$, $LM \parallel CB$

$$\therefore \frac{AM}{AB} = \frac{AL}{AC} \text{ [Basic Proportionality theorem]}$$

And in $\triangle ACD$, $LN \parallel CD$

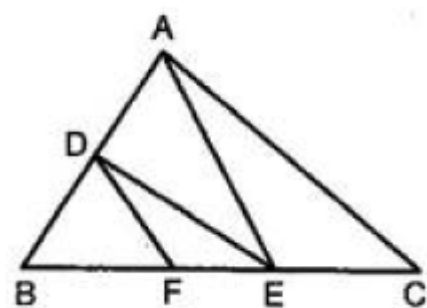
$$\therefore \frac{AL}{AC} = \frac{AN}{AD} \text{ [Basic Proportionality theorem]}$$

From eq. (i) and (ii), we have

$$\frac{AM}{AB} = \frac{AN}{AD}$$

Ex 6.2 Question 4.

In the given figure, $DE \parallel AC$ and $DF \parallel AE$. Prove that $\frac{BF}{FE} = \frac{BE}{EC}$.



Answer.

In $\triangle BCA$, $DE \parallel AC$

$$\therefore \frac{BE}{EC} = \frac{BD}{DA} \text{ [Basic Proportionality theorem]}$$

And in $\triangle BEA$, $DF \parallel AE$

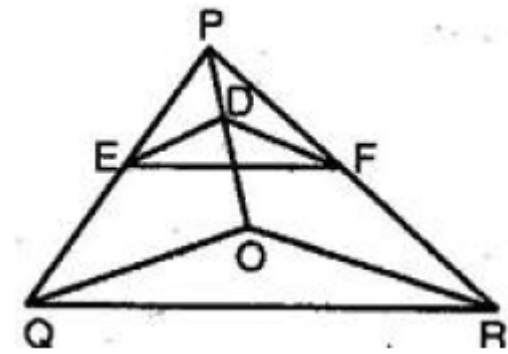
$$\therefore \frac{BF}{FE} = \frac{BD}{DA} \text{ [Basic Proportionality theorem]}$$

From eq. (i) and (ii), we have

$$\frac{BF}{FE} = \frac{BE}{EC}$$

Ex 6.2 Question 5.

In the given figure, $DE \parallel OQ$ and $DF \parallel OR$. Show that $EF \parallel QR$.



Answer.

In $\triangle PQO$, $DE \parallel OQ$

$$\therefore \frac{PE}{EQ} = \frac{PD}{DO} \text{ [Basic Proportionality theorem]}$$

And in $\triangle POR$, $DF \parallel OR$

$$\therefore \frac{PD}{DO} = \frac{PF}{FR} \text{ [Basic Proportionality theorem]}$$

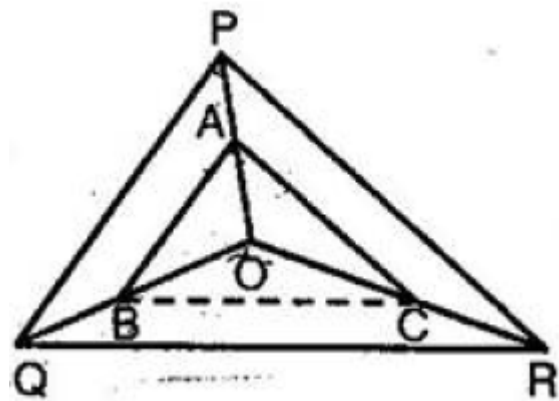
From eq. (i) and (ii), we have

$$\frac{PE}{EQ} = \frac{PF}{FR}$$

$$\therefore EF \parallel QR \text{ [By the converse of BPT]}$$

Ex 6.2 Question 6.

In the given figure, A , B , and C are points on OP , OQ and OR respectively such that $AB \parallel PQ$ and $AC \parallel PR$. Show that $BC \parallel QR$.



Answer.

Given: O is any point in $\triangle PQR$, in which $AB \parallel PQ$ and $AC \parallel PR$.

To prove: $BC \parallel QR$

Construction: Join BC .

Proof: In $\triangle OPQ$, $AB \parallel PQ$

$$\therefore \frac{OA}{AP} = \frac{OB}{BQ} \text{ [Basic Proportionality theorem]}$$

And in $\triangle OPR$, $AC \parallel PR$

$$\therefore \frac{OA}{AP} = \frac{OC}{CR} \text{ [Basic Proportionality theorem].}$$

From eq. (i) and (ii), we have

$$\frac{OB}{BQ} = \frac{OC}{CR}$$

\therefore In $\triangle OQR$, B and C are points dividing the sides OQ and OR in the same ratio.

\therefore By the converse of Basic Proportionality theorem,

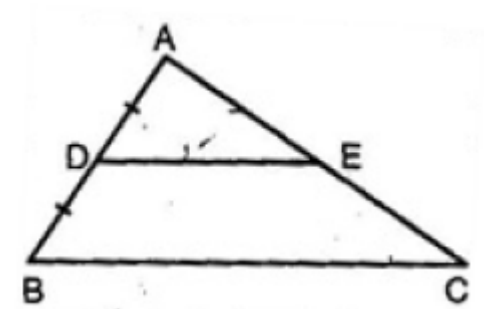
$$\Rightarrow BC \parallel QR$$

Ex 6.2 Question 7.

Using Theorem 6.1, prove that a line drawn through the midpoint of one side of a triangle parallel to another side bisects the third side. (Recall that you have proved it in Class IX).

Answer.

Given: A triangle ABC , in which D is the midpoint of side AB and the line DE is drawn parallel to BC , meeting AC at E .



To prove: $AE = EC$

Proof: Since $DE \parallel BC$

$\therefore \frac{AD}{DB} = \frac{AE}{EC}$ [Basic Proportionality theorem]

But $AD = DB$ [Given]

$$\Rightarrow \frac{AD}{DB} = 1$$

$$\Rightarrow \frac{AE}{EC} = 1 \text{ [From eq. (i)]}$$

$$\Rightarrow AE = EC$$

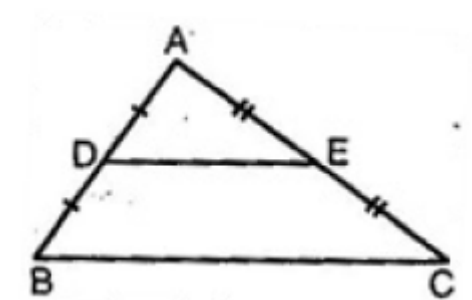
Hence, E is the midpoint of the third side AC.

Ex 6.2 Question 8.

Using Theorem 6.2, prove that the line joining the midpoints of any two sides of a triangle is parallel to the third side. (Recall that you have done it in Class IX).

Answer.

Given: A triangle ABC, in which D and E are the midpoints of sides AB and AC respectively.



To Prove: $DE \parallel BC$

Proof: Since D and E are the midpoints of AB and AC respectively.

$\therefore AD = DB$ and $AE = EC$

Now, $AD = DB$

$$\Rightarrow \frac{AD}{DB} = 1 \text{ and } AE = EC$$

$$\Rightarrow \frac{AE}{EC} = 1$$

$$\therefore \frac{AD}{DB} = \frac{AE}{EC} = 1$$

$$\Rightarrow \frac{AD}{DB} = \frac{AE}{EC}$$

Thus, in triangle ABC, D and E are points dividing the sides AB and AC in the same ratio.

Therefore, by the converse of Basic Proportionality theorem, we have

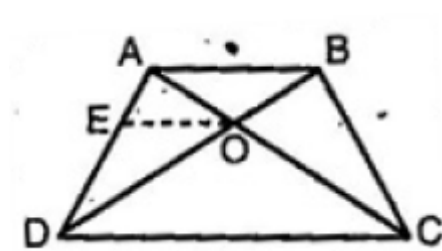
$DE \parallel BC$

Ex 6.2 Question 9.

ABCD is a trapezium in which $AB \parallel DC$ and its diagonals intersect each other at the point O. Show that $\frac{AO}{BO} = \frac{CO}{DO}$.

Answer.

Given: A trapezium ABCD, in which $AB \parallel DC$ and its diagonals AC and BD intersect each other at O.



To Prove: $\frac{AO}{BO} = \frac{CO}{DO}$

Construction: Through O, draw $OE \parallel AB$, i.e. $OE \parallel DC$.

Proof: In $\triangle ADC$, we have $OE \parallel DC$

$$\therefore \frac{AE}{ED} = \frac{AO}{CO} \text{ [By Basic Proportionality theorem]}$$

Again, in $\triangle ABD$, we have $OE \parallel AB$ [Construction]

$$\therefore \frac{ED}{AE} = \frac{DO}{BO} \text{ [By Basic Proportionality theorem]}$$

$$\Rightarrow \frac{AE}{ED} = \frac{BO}{DO}$$

From eq. (i) and (ii), we get

$$\frac{AO}{CO} = \frac{BO}{DO}$$

$$\Rightarrow \frac{AO}{BO} = \frac{CO}{DO}$$

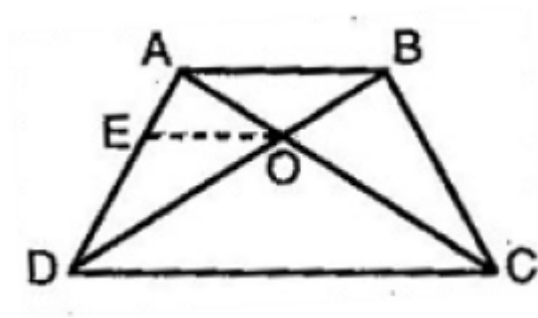
Ex 6.2 Question 10.



The diagonals of a quadrilateral $ABCD$ intersect each other at the point O such that $\frac{AO}{BO} = \frac{CO}{DO}$. Show that $ABCD$ is a trapezium.

Answer.

Given: A quadrilateral $ABCD$, in which its diagonals AC and BD intersect each other at O such that $\frac{AO}{BO} = \frac{CO}{DO}$, i.e.



$$\frac{AO}{CO} = \frac{BO}{DO}$$

To Prove: Quadrilateral $ABCD$ is a trapezium.

Construction: Through O , draw $OE \parallel AB$ meeting AD at E .

Proof: In $\triangle ADB$, we have $OE \parallel AB$ [By construction]

$$\therefore \frac{DE}{EA} = \frac{DO}{BO} \text{ [By Basic Proportionality theorem]}$$

$$\Rightarrow \frac{EA}{DE} = \frac{BO}{DO}$$

$$\Rightarrow \frac{EA}{DE} = \frac{BO}{DO} = \frac{AO}{CO}$$

$$\left[\therefore \frac{AO}{CO} = \frac{BO}{DO} \right]$$

$$\Rightarrow \frac{EA}{DE} = \frac{AO}{CO}$$

Thus in $\triangle ADC$, E and O are points dividing the sides AD and AC in the same ratio. Therefore by the converse of Basic Proportionality theorem, we have

$$EO \parallel DC$$

But $EO \parallel AB$ [By construction]

$$\therefore AB \parallel DC$$

\therefore Quadrilateral $ABCD$ is a trapezium

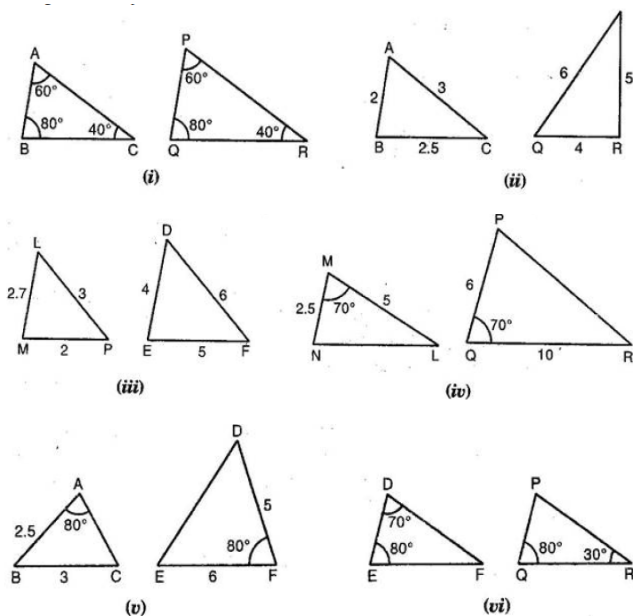
Exercise 6.3 (Revised) - Chapter 6 - Triangles - Ncert Solutions class 10 - Maths

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Chapter 6 Triangles NCERT Solutions Class 10 Maths: Simplify Concepts & Ace Exams

Ex 6.3 Question 1.

State which pairs of triangles in the given figure, are similar. Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



Answer.

(i) In $\triangle ABC$ and $\triangle PQR$, we observe that,

$$\angle A = \angle P = 60^\circ, \angle B = \angle Q = 80^\circ \text{ and } \angle C = \angle R = 40^\circ$$

\therefore By AAA criterion of similarity, $\triangle ABC \sim \triangle PQR$

(ii) In $\triangle ABC$ and $\triangle PQR$, we observe that,

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{CA}{PR} = \frac{1}{2}$$

\therefore By SSS criterion of similarity, $\triangle ABC \sim \triangle PQR$

(iii) In $\triangle LMP$ and $\triangle DEF$, we observe that the ratio of the sides of these triangles is not equal.

Therefore, these two triangles are not similar.

(iv) In $\triangle MNL$ and $\triangle PQR$, we observe that, $\angle M = \angle Q = 70^\circ$

$$\text{But, } \frac{MN}{PQ} \neq \frac{ML}{QR}$$

\therefore These two triangles are not similar as they do not satisfy SAS criterion of similarity.

(v) In $\triangle ABC$ and $\triangle DEF$, we have, $\angle A = \angle F = 80^\circ$

$$\text{But, } \frac{AB}{DE} \neq \frac{AC}{DF} [\because AC \text{ is not given}]$$

\therefore These two triangles are not similar as they do not satisfy SAS criterion of similarity.

(vi) In $\triangle DEF$ and $\triangle PQR$, we have, $\angle D = \angle P = 70^\circ$

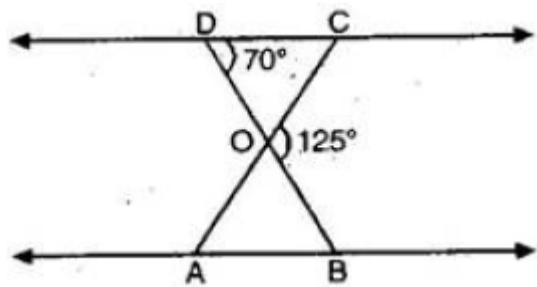
$$[\because \angle P = 180^\circ - 80^\circ - 30^\circ = 70^\circ]$$

$$\text{And } \angle E = \angle Q = 80^\circ$$

\therefore By AAA criterion of similarity, $\triangle DEF \sim \triangle PQR$

Ex 6.3 Question 2.

In figure, $\triangle ODC \sim \triangle OBA$, $\angle BOC = 125^\circ$ and $\angle CDO = 70^\circ$. Find $\angle DOC$, $\angle DCO$ and $\angle OAB$.



Answer.

Since BD is a line and OC is a ray on it.

$$\therefore \angle DOC + \angle BOC = 180^\circ$$

$$\Rightarrow \angle DOC + 125^\circ = 180^\circ$$

$$\Rightarrow \angle DOC = 55^\circ$$

In $\triangle CDO$, we have $\angle CDO + \angle DOC + \angle DCO = 180^\circ$

$$\Rightarrow 70^\circ + 55^\circ + \angle DCO = 180^\circ$$

$$\Rightarrow \angle DCO = 55^\circ$$

It is given that $\triangle ODC \sim \triangle OBA$

$$\therefore \angle OBA = \angle ODC, \angle OAB = \angle OCD$$

$$\Rightarrow \angle OBA = 70^\circ, \angle OAB = 55^\circ$$

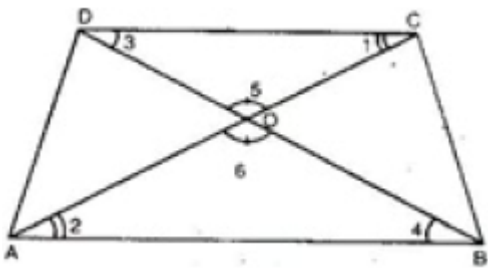
Hence $\angle DOC = 55^\circ$, $\angle DCO = 55^\circ$ and $\angle OAB = 55^\circ$

Ex 6.3 Question 3.

Diagonals AC and BD of a trapezium $ABCD$ with $AB \parallel CD$ intersect each other at the point O . Using a similarity criterion for two triangles, show that $\frac{OA}{OC} = \frac{OB}{OD}$

Answer.

Given: $ABCD$ is a trapezium in which $AB \parallel DC$.



To Prove: $\frac{OA}{OC} = \frac{OB}{OD}$

Proof: In $\triangle OAB$ and OCD , we have,

$$\angle 5 = \angle 6 \text{ [Vertically opposite angles]}$$

$$\angle 1 = \angle 2 \text{ [Alternate angles]}$$

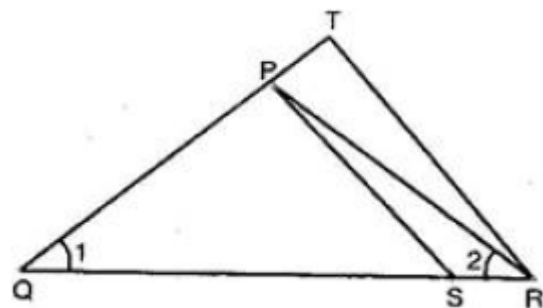
$$\text{And } \angle 3 = \angle 4 \text{ [Alternate angles]}$$

\therefore By AAA criterion of similarity, $\triangle OAB \sim \triangle ODC$

$$\text{Hence, } \frac{OA}{OC} = \frac{OB}{OD}$$

Ex 6.3 Question 4.

In figure, $\frac{QR}{QS} = \frac{QT}{PR}$ and $\angle 1 = \angle 2$. Show that $\triangle PQS \sim \triangle TQR$.



Answer.

$$\text{We have, } \frac{QR}{QS} = \frac{QT}{PR}$$

$$\Rightarrow \frac{QT}{QR} = \frac{PR}{QS}$$

$$\text{Also, } \angle 1 = \angle 2 \text{ [Given]}$$

$$\therefore PR = PQ \quad (2) \text{ [}\because \text{Sides opposite to equal } \angle\text{s are equal]}$$

From eq.(1) and (2), we get

$$\frac{QT}{QR} = \frac{PR}{QS} \Rightarrow \frac{PQ}{QT} = \frac{QS}{QR}$$

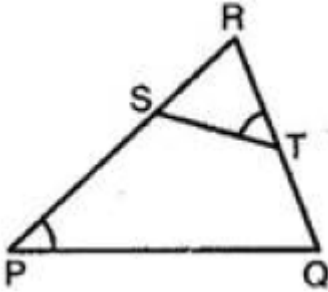
In Δ s PQS and TQR, we have,
 $\frac{PQ}{QT} = \frac{QS}{QR}$ and $\angle PQS = \angle TQR = \angle Q$
 \therefore By SAS criterion of similarity, $\Delta PQS \sim \Delta TQR$

Ex 6.3 Question 5.

S and T are points on sides PR and QR of a ΔPQR such that $\angle P = \angle RTS$. Show that $\Delta RPQ \sim \Delta RTS$.

Answer.

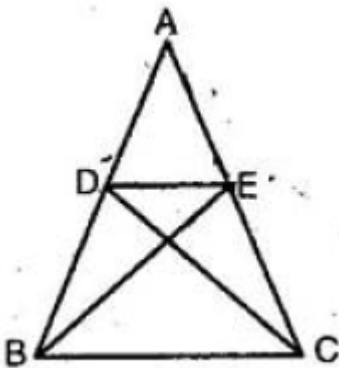
In Δ s RPQ and RTS, we have



$\angle RPQ = \angle RTS$ [Given]
 $\angle PRQ = \angle TRS$ [Common]
 \therefore By AA-criterion of similarity,
 $\Delta RPQ \sim \Delta RTS$

Ex 6.3 Question 6.

In the given figure, if $\Delta ABE \cong \Delta ACD$, show that $\Delta ADE \sim \Delta ABC$.



Answer.

It is given that $\Delta ABE \cong \Delta ACD$
 $\therefore AB = AC$ and $AE = AD$

$$\Rightarrow \frac{AB}{AD} = \frac{AC}{AE}$$

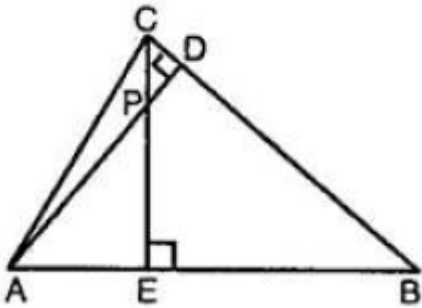
$$\Rightarrow \frac{AB}{AC} = \frac{AD}{AE} \dots \dots \dots (1)$$

\therefore In Δ s ADE and ABC, we have,
 $\frac{AB}{AC} = \frac{AD}{AE}$ [from eq.(1)]

And $\angle BAC = \angle DAE$ [Common]
Thus, by SAS criterion of similarity, $\Delta ADE \sim \Delta ABC$

Ex 6.3 Question 7.

In figure, altitude AD and CE of a ΔABC intersect each other at the point P . Show that:



- (i) $\Delta AEP \sim \Delta CDP$
- (ii) $\Delta ABD \sim \Delta CBE$
- (iii) $\Delta AEP \sim \Delta ADB$
- (iv) $\Delta PDC \sim \Delta BEC$

Answer.

(i) In Δ s AEP and CDP, we have,
 $\angle AEP = \angle CDP = 90^\circ$ [$\because CE \perp AB, AD \perp BC$]
And $\angle APE = \angle CPD$ [Vertically opposite]
 \therefore By AA-criterion of similarity, $\Delta AEP \sim \Delta CDP$
(ii) In Δ s AABD and CBE, we have,
 $\angle ADB = \angle CEB = 90^\circ$

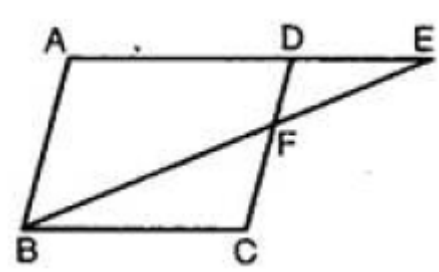
And $\angle ABD = \angle CBE$ [Common]
 \therefore By AA-criterion of similarity, $\triangle ABD \sim \triangle CBE$
 (iii) In \triangle s AEP and ADB, we have,
 $\angle AEP = \angle ADB = 90^\circ$ [$\because AD \perp BC, CE \perp AB$]
 And $\angle PAE = \angle DAB$ [Common]
 \therefore By AA-criterion of similarity, $\triangle AEP \sim \triangle ADB$
 (iv) In \triangle s PDC and BEC, we have,
 $\angle PDC = \angle BEC = 90^\circ$ [$\because CE \perp AB, AD \perp BC$]
 And $\angle PCD = \angle BEC$ [Common]
 \therefore By AA-criterion of similarity, $\triangle PDC \sim \triangle BEC$

Ex 6.3 Question 8.

E is a point on the side AD produced of a parallelogram $ABCD$ and BE intersects CD at F. Show that $\triangle ABE \sim \triangle CFB$.

Answer.

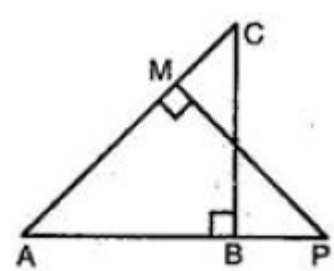
In \triangle s ABE and CFB, we have,



$\angle AEB = \angle CBF$ [Alt. \angle s]
 $\angle A = \angle c$ [opp. \angle s of a ||gm]
 \therefore By AA-criterion of similarity, we have
 $\triangle ABE \sim \triangle CFB$

Ex 6.3 Question 9.

In the given figure, ABC and AMP are two right triangles, right angles at B and M respectively. Prove that:



- (i) $\triangle ABC \sim \triangle AMP$
- (ii) $\frac{CA}{PA} = \frac{BC}{MP}$

Answer.

(i) In \triangle s ABC and AMP , we have,
 $\angle ABC = \angle AMP = 90^\circ$ [Given]
 $\angle BAC = \angle MAP$ [Common angles]
 \therefore By AA-criterion of similarity, we have
 $\triangle ABC \sim \triangle AMP$

- (ii) We have $\triangle ABC \sim \triangle AMP$ [As prove above]
 $\Rightarrow \frac{CA}{PA} = \frac{BC}{MP}$

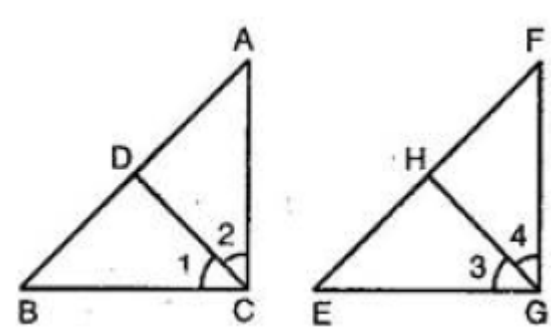
Ex 6.3 Question 10.

CD and GH are respectively the bisectors of $\angle ACB$ and $\angle EGF$ such that D and H lie on sides AB and FE at $\triangle ABC$ and $\triangle EFG$ respectively. If $\triangle ABC \sim \triangle FEG$, show that:

- (i) $\frac{CD}{GH} = \frac{AC}{FG}$
- (ii) $\triangle DCB \sim \triangle HE$
- (iii) $\triangle DCA \sim \triangle HGF$

Answer.

We have, $\triangle ABC \sim \triangle FEG$



$$\Rightarrow \angle A = \angle F \dots\dots\dots (1)$$

And $\angle C = \angle G$

$$\Rightarrow \frac{1}{2}\angle C = \frac{1}{2}\angle G$$

$$\Rightarrow \angle 1 = \angle 3 \text{ and } \angle 2 = \angle 4 \dots\dots\dots (2)$$

[\because CD and GH are bisectors of $\angle C$ and $\angle G$ respectively]

\therefore In Δ s DCA and HGF, we have

$$\angle A = \angle F \text{ [From eq.(1)]}$$

[\because CD and GH are bisectors of $\angle C$ and $\angle G$ respectively]

\therefore In Δ s DCA and HGF, we have

$$\angle 2 = \angle 4 \text{ [From eq.(2)]}$$

\therefore By AA-criterion of similarity, we have

$$\Delta DCA \sim \Delta HGF$$

Which proves the (iii) part

We have, $\Delta DCA \sim \Delta HGF$

$$\Rightarrow \frac{AG}{FG} = \frac{CD}{GH}$$

$$\Rightarrow \frac{CD}{GH} = \frac{AC}{FG}$$

Which proves the (i) part

In Δ s DCA and HGF, we have

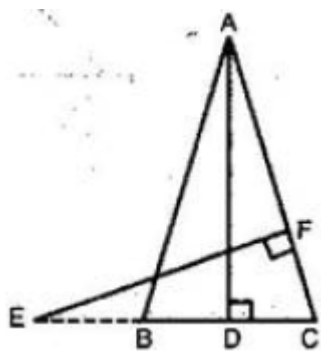
$$\angle 1 = \angle 3 \text{ [From eq.(2)]}$$

$$\angle B = \angle E \text{ [}\because \Delta DCB \sim \Delta HE\text{]}$$

Which proves the (ii) part

Ex 6.3 Question 11.

In the given figure, E is a point on side CB produced of an isosceles triangle ABC with $AB = AC$. If $AD \perp BC$ and $EF \perp AC$, prove that $\Delta ABD \sim \Delta ECF$.



Answer.

Here ΔABC is isosceles with $AB = AC$

$$\therefore \angle B = \angle C$$

In Δ s ABD and ECF , we have

$$\angle ABD = \angle ECF \text{ [}\because \angle B = \angle C\text{]}$$

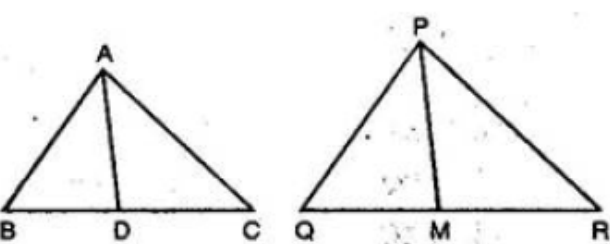
$$\angle ABD = \angle ECF = 90^\circ \text{ [}\because AD \perp BC \text{ and } EF \perp AC\text{]}$$

\therefore By AA-criterion of similarity, we have

$$\Delta ABD \sim \Delta ECF$$

Ex 6.3 Question 12.

Sides AB and BC and median AD of a triangle ABC are respectively proportional to sides PQ and QR and median PM of a ΔPQR (see figure). Show that $\Delta ABC \sim \Delta PQR$.



Answer.

Given: AD is the median of ΔABC and PM is the median of ΔPQR such that

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AD}{PM}$$

To prove: $\Delta ABC \sim \Delta PQR$

$$\text{Proof: } BD = \frac{1}{2}BC \text{ [Given]}$$

$$\text{And } QM = \frac{1}{2}QR \text{ [Given]}$$

Also $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AD}{PM}$ [Given]
 $\Rightarrow \frac{AB}{PQ} = \frac{2BD}{2QM} = \frac{AD}{PM}$
 $\Rightarrow \frac{AB}{PQ} = \frac{BD}{QM} = \frac{AD}{PM}$
 $\therefore \triangle ABD \sim \triangle PQM$ [By SSS-criterion of similarity]
 $\Rightarrow \angle B = \angle Q$ [Similar triangles have corresponding angles equal]
 And $\frac{AB}{PQ} = \frac{BC}{QR}$ [Given]

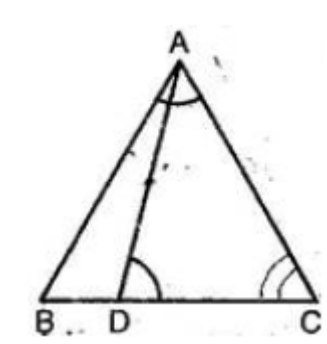
And $\frac{AB}{PQ} = \frac{BC}{QR}$ [Given]
 \therefore By SAS-criterion of similarity, we have
 $\triangle ABC \sim \triangle PQR$

Ex 6.3 Question 13.

D is a point on the side BC of a triangle ABC such that $\angle ADC = \angle BAC$. Show that $CA^2 = CB \cdot CD$.

Answer.

In triangles ABC and DAC,



$\angle ADC = \angle BAC$ [Given]
 and $\angle c = \angle C$ [Common]
 \therefore By AA-similarity criterion,
 $\triangle ABC \sim \triangle DAC$
 $\Rightarrow \frac{AB}{DA} = \frac{BC}{AC} = \frac{AC}{DC}$
 $\Rightarrow \frac{CB}{CA} = \frac{CA}{CD}$

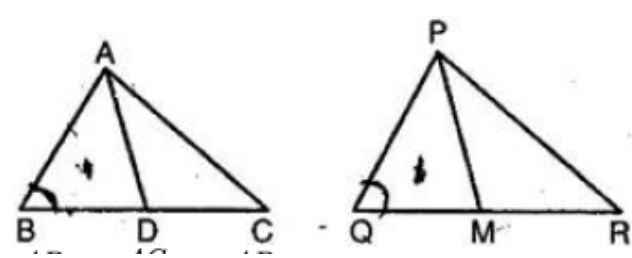
$\Rightarrow CA^2 = CB \cdot CD$

Ex 6.3 Question 14.

Sides AB and AC and median AD of a triangle ABC are respectively proportional to sides PQ and PR and median PM of another triangle PQR . Show that $\triangle ABC \sim \triangle PQR$.

Answer.

Given: AD is the median of $\triangle ABC$ and PM is the median of $\triangle PQR$ such that

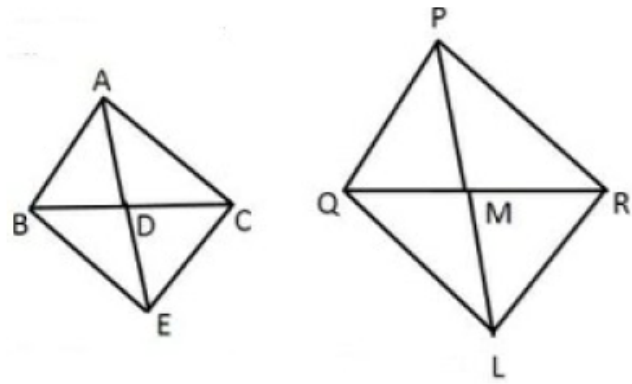


$\frac{AB}{PQ} = \frac{AC}{PR} = \frac{AD}{PM}$ (1)

To prove: $\triangle ABC \sim \triangle PQR$

Proof:

Let us extend AD to point D such that $AD = DE$ and PM up to point L such that $PM = ML$



Join B to E. C to E,and Q to L, and R to L
 We know that medians is the bisector of opposite side
 Hence
 $BD = DC$

Also, AD = DE (by construction)

Hence in quadrilateral ABEC, diagonals AE and BC bisect each other at point D. Therefore, quadrilateral ABEC is a parallelogram.

AC = BE

AB = EC (opposite sides of \parallel gm are equal)

Similarly, we can prove that PQLR is a parallelogram

PR = QL

PQ = LR opposite sides of \parallel gm are equal)

Given that

AB/PQ = AC/PR = AD/PM

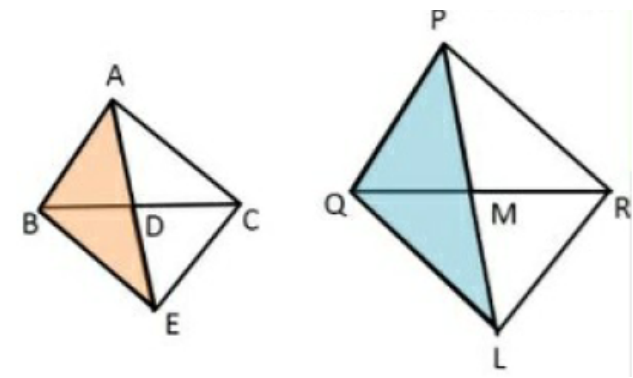
AB/PQ = BE/QL = AD/PM [from (2) (3)]

AB/PQ = BE/QL = 2AD/2PM

AB/PQ = BE/QL = AE/PL [as AD = DE, AE = AD + DE = 2AD

PM = ML \cdot PL = PM + ML = 2PM

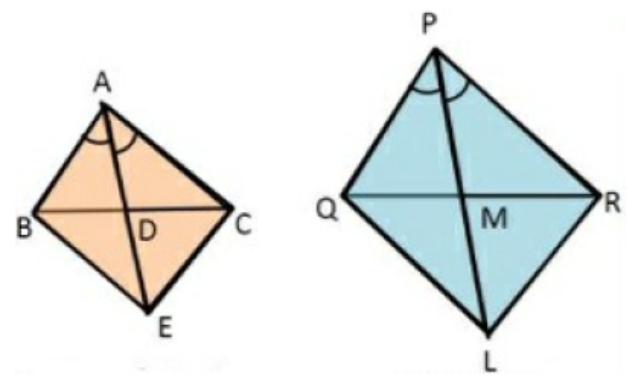
\triangle ABE \sim \triangle PQL (By SSS Similiarity Criteria)



We know that corresponding angles of similar triangles are equal.

\angle BAE = \angle QPL(4)

Similarly, we can prove that \triangle AEC \sim \triangle PLR.



We know that corresponding angles of similar triangles are equal.

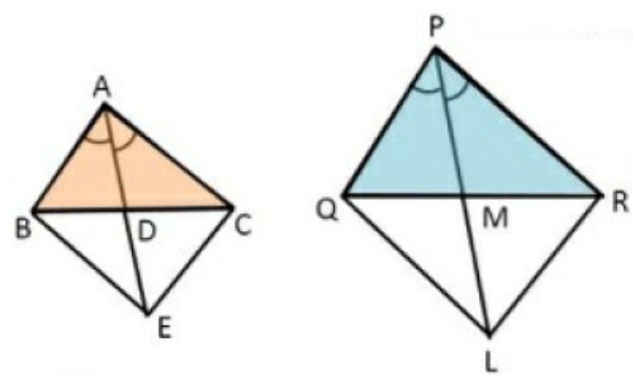
\angle CAE = \angle RPL (5)

Adding (4) and (5),

\angle BAE + \angle CAE = \angle QPL + \angle RPL

\angle CAB = \angle RPQ

In \triangle ABC and \triangle PQR



AB/PQ = AC/PR

\angle CAB = \angle RPQ

\triangle ABC \sim \triangle PQR

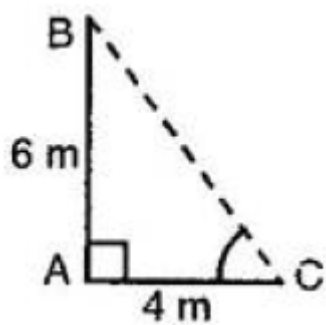
Hence proved

Ex 6.3 Question 15.

A vertical pole of length 6 m casts a shadow 4 m long on the ground and at the same time a tower casts a shadow 28 m long. Find the height of the tower.

Answer.

Let AB be the vertical pole and AC be its shadow. Also, let DE be the vertical tower and DF be its shadow. Joined BC and EF.



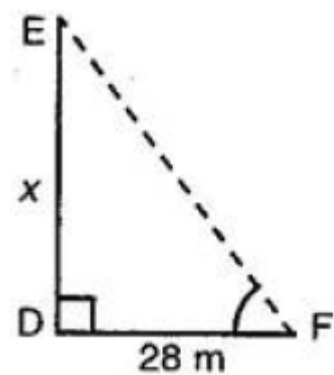
Let $DE = x$ meters

Here, $AB = 6$ m, $AC = 4$ m and $DF = 28$ m

In the triangles ABC and DEF,

$\angle A = \angle D = 90^\circ$

And $\angle C = \angle F$ [Each is the angular elevation of the sun]



\therefore By AA-similarity criterion,

$\triangle ABC \sim \triangle DEF$

$$\Rightarrow \frac{AB}{DE} = \frac{AC}{DF}$$

$$\Rightarrow \frac{6}{x} = \frac{4}{28}$$

$$\Rightarrow \frac{6}{x} = \frac{1}{7}$$

$$\Rightarrow x = 42 \text{ m}$$

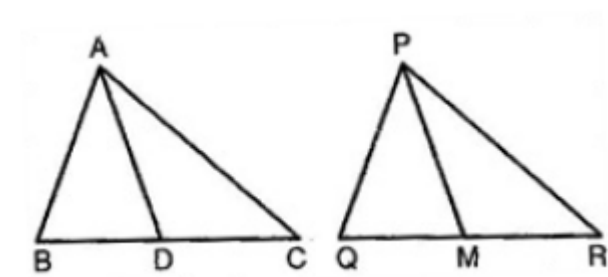
Hence, the height of the tower is 42 meters.

Ex 6.3 Question 16.

If AD and PM are medians of triangles ABC and PQR respectively, where $\triangle ABC \sim \triangle PQR$, prove that $\frac{AB}{PQ} = \frac{AD}{PM}$

Answer.

Given: AD and PM are the medians of triangles ABC and PQR respectively, where



$\triangle ABC \sim \triangle PQR$

To prove: $\frac{AB}{PQ} = \frac{AD}{PM}$

Proof: In triangles ABD and PQM,

$\angle B = \angle Q$ [Given]

And $\frac{AB}{PQ} = \frac{\frac{1}{2}BC}{\frac{1}{2}QR}$ [\because AD and PM are the medians of BC and QR respectively]

$$\Rightarrow \frac{AB}{PQ} = \frac{BD}{QM}$$

\therefore By SAS-criterion of similarity,

$\triangle ABD \sim \triangle PQM$

$$\Rightarrow \frac{AB}{PQ} = \frac{BD}{QM} = \frac{AD}{PM}$$

$$\Rightarrow \frac{AB}{PQ} = \frac{AD}{PM}$$